

Volume 3

Rudolf Och

SPLINES

STANDARDS AND CALCULATION

*learn
teach
consult*




*pure
perfection*

FRENCO

The author

Graduate Engineer (Dipl. Ing., FH) Rudolf Och was born in Bamberg, Germany in 1951. After graduating in mechanical engineering he founded FRESCO GmbH in Nuremberg, Germany in 1978. In the beginning, the company only engaged in the development and manufacture of spline gauges. Over the years, however, the business was extended to include the full spectrum of gear and spline metrology. This development is supported by numerous inventions.

The author was a member of the American Standards Institute for Splines ANSI and has been Chairman of the German standards committee AA 2.1 since 1993. During the chairmanship, the German term for spline (Passverzahnung) was officially introduced and all relevant German standards were revised. The international standard ISO 4156 was also completely revised under German leadership by the responsible standards committee ISO/TC 14.

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Preface

Splines are a difficult technical “marginal area” within drive technology. They are neither addressed during vocational training nor in degree courses. Experts in the matter are accordingly few and far between. There is an undeniable diversity of official spline standards and internal company standards, some of which are incomplete and others plainly wrong. Some, however, do comply with the current state of technology. This book provides an overview of the standards, which is otherwise difficult to obtain.

This book is a compilation of individual documentations, which were compiled over a period of 30 years from the author’s experiences. It was revised as a whole before print and reflects the status quo of standardisation.

Commonly used formulae are described in a simple manner at the end of the book. These formulae only apply to spur gearing without helix angle.

No responsibility is accepted for the accuracy of the information in this book. It must be noted, however, that technical developments are a continuous process and knowledge, standards and rules are subject to constant changes.

June 2008, Rudolf Och

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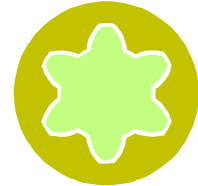
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1. List of Standards (formerly OFS 24)

National and International
Works standards
Modification of standards
Valid and invalid standards

1.1. Involute splines



| Standard | Publisher | Content | Version | Note |
|----------------|----------------|--|---------|---|
| ASA B 5.15 | USA | Involute splines and serrations | 1960 | Predecessor of ANSI B 92.1 |
| ANSI B 92.1 | USA | Involute Splines | 1996 | |
| ANSI B 92.1b | USA | Involute Splines Addendum | 1996 | Amendment |
| ANSI B 92.2M | USA | Metric Module Involute Splines | 1989 | Similar to ISO 4156 - 1981 |
| ASAE S 203.12 | USA | Rear power Takeoff for agricultural tractors | 1994 | Similar to DIN 9611, but with different fits |
| SAE J498 | USA | Involute splines | | Similar to ANSI B 92.1 |
| ANT 2020 | Sulzer | Zoll-Vielkeilverbindungen mit Evolventenflanken | 1968 | |
| BS 3550 | England | Involute Splines | 1963 | Similar to ANSI B92.1 |
| BS 6186 | England | Involute Splines: Metric module side fit | 1981 | = ISO 4156 - 1981 |
| BS ISO 4156 | England | Involute Splines: Metric module side shift | 2006 | English version of ISO 4156 - 2005 |
| CSN 01 4952-54 | Czech Republic | Involute splines | 1981 | Pressure angle 30° |
| DIN 5466-1 | Germany | Tragfähigkeitsberechnung von Zahn- und Keilwellen-Verbindungen | 2000 | |
| DIN 5466-2 | Germany | Tragfähigkeitsberechnung von Zahnwellen- und Keilwellen-Verbindungen nach DIN 5480 | 2002 | Draft version |
| DIN 5480 | Germany | Passverzahnungen mit Evolventenflanken | 2006 | |
| DIN 5482 | Germany | Zahnradprofile- und Zahnwellen-Profile mit Evolventenflanken | 1973 | Withdrawn |
| DIN 9611 | Germany | Heckzapfwelle | 1992 | Is ISO 500 |
| 01.30.4008 | Renault | Cannelures Cylindriques Droites a Flancs en Développante | 1984 | Pressure angle 20°, with effective tolerances |

| Standard | Publisher | Content | Version | Note |
|---------------|---------------|---|---------|--|
| E22-141 | France | Cannelures Rectilignes a flancs en développant | 1955 | Pressure angle 20°, without effective tolerances |
| E22-142 | France | Cannelures cylindriques droites a flancs en développant | 1986 | Gauges for E22-141 |
| E22-144 | France | Cannelures cylindriques droites a flancs an développant, généralités | 1978 | The equivalent of ISO 4156 - 1981 |
| E22-145 | France | Cannelures cylindriques droites a flancs an développante, vérification | 1979 | The equivalent of ISO 4156 |
| NF ISO 4156 | France | Cannelures cylindriques droites a flancs developpante | 2006 | French edition of ISO 4156 |
| CTD-STD-1509 | GKN-Cardantec | Involute splines | 1989 | Similar to DIN 5480, but with a 25° pressure angle |
| Fiat 63350-54 | Fiat | Profillehren für Zahn- und Zahnwellenprofile mit Evolventen ASA | 1964 | |
| HES A1013-73 | Honda | Involute splines | 1976 | Pressure angle 37.5°, reference to JIS D2001 |
| ISO 500 | International | Heckzapfwelle | | Previously DIN 9611 |
| ISO 4156 | International | Straight cylindrical involute splines | 2005 | |
| ISO/DP 8399/2 | International | Aéronautique et espace | 1986 | Excerpt from ISO 4156 |
| JIS B 1602 | Japan | Involute serrations | 1961 | Pressure angle 45° |
| JIS B 1603 | Japan | Straight cylindrical involute splines | 1995 | = ISO 4156 - 1981 old + excerpts from D 2001 |
| JIS D 2001 | Japan | Involute Spline for Automobiles | 1959 | Withdrawn 1995, partly included in B1603 |
| KHD 0099-40 | KHD | Evolventische Vielkeilprofile | 1969 | |
| LaN 745 | John Deere | Verzahnungsdaten | 1990 | |
| N06.030 | Hydromatik | Keilwellen-Verbindungen mit Evolventenflanken nach ANSI B92.1a Sonderausführungen | 1954 | |
| NSE 506.04 | D. Airbus | | 1968 | Similar to E22-141 |
| R18 | Rolls-Royce | Tooth control for Involute Splines | 1976 | Based on B92.1 |
| SMS 1830 | Sweden | Bomförband med evolventprofil | 1958 | Similar to ASA B5.15 |
| SMS 1833-36 | Sweden | Bomförband med evolventprofil | 1958 | DP, pressure angle 30° |
| ST 2514 | Turbomeca | Straight cylindrical involute splines | 1980 | Extract from E22-145 |

| Standard | Publisher | Content | Version | Note |
|-----------------|------------------|---|----------------|-------------------------------|
| TGL 5482 | East Germany | Zahnnabenprofile- und Zahnwellenprofile mit Evolventenflanken | 1979 | The equivalent of DIN 5482 |